

Today in CS5:

`chr(9829)`

# The ♥ of CS (and CSers...)

## *Algorithms!*



*I feel at home with  
recursion now!*



# Caesar Cipher: **encipher**

**encipher** ( **s** , **n** )

should return the string **s** with each *alphabetic* character shifted/wrapped by **n** places in the alphabet

`encipher( 'I <3 Latin' , 0 )`  $\xrightarrow{\text{returns}}$  `'I <3 Latin'`

`encipher( 'I <3 Latin' , 1 )`  $\xrightarrow{\text{returns}}$  `'J <3 Mbujo'`

`encipher( 'I <3 Latin' , 2 )`  $\xrightarrow{\text{returns}}$  `'K <3 Ncvkp'`

`encipher( 'I <3 Latin' , 3 )`  $\xrightarrow{\text{returns}}$  `'L <3 Odwlq'`

`encipher( 'I <3 Latin' , 4 )`  $\xrightarrow{\text{returns}}$  `'M <3 Pexmr'`

`encipher( 'I <3 Latin' , 5 )`  $\xrightarrow{\text{returns}}$  `'N <3 Qfyns'`

⋮

*Algorithm 0*

`encipher( 'I <3 Latin' , 25 )`  $\xrightarrow{\text{returns}}$  `'H <3 Kzshm'`

# Caesar Cipher: encipher

**encipher** (**s**, **n**)

should return the string **s** with each *alphabetic* character shifted/wrapped by **n** places in the alphabet

`encipher( 'I <3 Latin' , 0 )`  $\xrightarrow{\text{returns}}$  `'I <3 Latin'`

`encipher( 'I <3 Latin' , 1 )`  $\xrightarrow{\text{returns}}$  `'J <3 Mbujo'`

`encipher( 'I <3 Latin' , 2 )`  $\xrightarrow{\text{returns}}$  `'K <3 Ncvkp'`

“...si qua occultius perferenda erant, per notas scripsit, id est sic structo litterarum ordine, ut nullum verbum effici posset; quae si qui investigare et persequi velit, quartam elementorum litteram, id est D pro A et perinde reliquas commutet...”

- Suetonius, *De Vitae Caesar*

“...if any were to be conveyed more secretly, he wrote in notes, that is, in such a structured order of letters that no word could be made; that is, he exchanges D for A and exchanges the rest in the same manner...”

- Suetonius, *The Life of Caesar*

*Design...*

*design of what?*

The ♥ of CS  
(and CSers...)

*Algorithms!*

*Design...*

*design of **what?***

*Code?*

*syntax*

# The Economist explains

## Explaining the world, daily



[Previous](#) | [Next](#) | [Latest The Economist explains](#)

[All latest updates](#)

The Economist explains

## What is code?

Sep 8th 2015, 23:50 BY T.S.



```
for i in people.data.users:
    response = client.api.statuses.user_timeline.get(screen_name=i.screen_name)
    print 'Got', len(response.data), 'tweets from', i.screen_name
    if len(response.data) != 0:
        ltdate = response.data[0]['created_at']
        ltdate2 = datetime.strptime(ltdate, '%a %b %d %H:%M:%S +0000 %Y')
        today = datetime.now()
        howlong = (today-ltdate2).days
        if howlong < daywindow:
            print i.screen_name, 'has tweeted in the past', daywindow,
            totaltweets += len(response.data)
            for j in response.data:
                if j.entities.urls:
                    for k in j.entities.urls:
                        newurl = k['expanded_url']
                        urlset.add((newurl, j.user.screen_name))
        else:
            print i.screen_name, 'has not tweeted in the past', daywindow
```



*Python!*

# The Economist explains

Explaining the world, daily

Previous | Next | Latest The Economist explains

The Economist explains

## What is code?

Sep 8th 2015, 23:50 BY T.S.

FROM lifts to cars to airliners to smartphones, modern civilisation is powered by software, the digital instructions that allow computers, and the devices they control, to perform calculations and respond to their surroundings. How did that software get there? Someone had to write it. But code, the sequences of symbols painstakingly created by programmers, is not quite the same as software, the sequences of instructions that computers execute. So what exactly is it?

*syntax*

Coding, or programming, is a way of writing instructions for computers that bridges the gap between how humans like to express themselves and how computers actually work.

Programming languages, of which there are hundreds, cannot generally be executed by computers directly. Instead, programs written in a particular "high level" language such as C++, Python or Java are translated by a special piece of software (a compiler or an interpreter) into low-level instructions which a computer can actually run. In some cases programmers write software in low-level instructions directly, but this is fiddly. It is usually much easier to use a high-level programming language, because such languages make it

```
for i in people.data.users:
    response = client.api.statuse
    print 'Got', len(response.dat
    if len(response.data) != 0:
        ltdate = response.data[0]
        ltdate2 = datetime.strptime(ltdate, '%a %b %d %H:%M:%S +0000 %Y
        today = datetime.now()
        howlong = (today-ltdate2).days
        if howlong < daywindow:
            print i.screen_name, 'has tweeted in the past' , daywindow,
            totaltweets += len(response.data)
            for j in response.data:
                if j.entities.urls:
                    for k in j.entities.urls:
                        newurl = k['expanded_url']
                        urlset.add((newurl, j.user.screen_name))
        else:
            print i.screen_name, 'has not tweeted in the past', daywind
```

*Python!*

*Design...*

*design of what?*

~~*Code?*~~

*syntax*

*Algorithms!*

*ideas!*



# Algorithm Design...

```
remAll (e, L)
```

*remove all e's from L*

# Design...

## *Top-down design*

Visualize

Split into parts

Build each part

Combine

Test

```
remAll (e, L)
```

*remove all e's from L*

```
remAll (42, [5, 7, 42, 8, 42])
```

```
[5, 7, 8]
```

```
remAll ('q', 'qaqqqlqqiqqqiieqqnqs')
```

```
'aliiens'
```

L1

L2

# Design...

Top-down  
design

Visualize

Split into parts

Build each part

Combine

Test

```
remAll (e, L)
```

*remove all e's from L*

Use it!

*it*

```
remAll (42, [5, 7, 42, 8, 42])
```

*'the rest'*

```
[5, 7, 8]
```

*'it'*

*L[0]* and *L[1:]*

*'the rest'*

*it*

```
remAll ('q', 'qaaqq1qqiqqiiqqnqs')
```

*'the rest'*

```
'aliiens'
```

Lose it!

# Design...

Top-down  
design

Visualize

Split into parts

Build each part

Combine

Test

```
remAll (e, L)
```

*remove all e's from L*

Use it!

*it*

```
remAll (42, [5, 7, 42, 8, 42])
```

*'the rest'*

*keep L[0]*

*+ remove e from the rest*

```
[5, 7, 8]
```

*it*

```
remAll ('q', 'qaaqqiqqiiqueqqnqs')
```

*'the rest'*

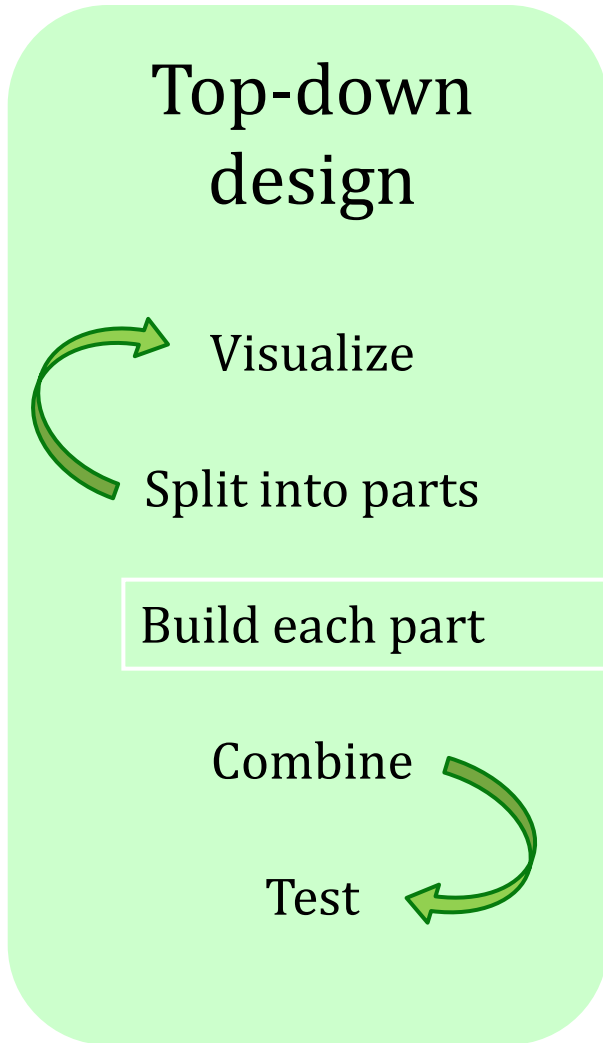
*drop L[0]*

*+ remove e from the rest*

```
'aliiens'
```

Lose it!

# Design...



```
remAll (e, L)
```

*remove all e's from L*

*Use it!*

*it*

```
remAll (L)
```

*keep L[0]  
+ remove e from*

**Use it!**

**- or -**

*it*

```
remAll ('q', 'xaxax')
```

*drop L[0]  
+ remove e from*

**Lose it.**

*Lose it!*

# Design ~ code

`remAll (e, L)`

*remove all e's from L*

Top-down  
design

Re-Visualize *in syntax!*?

```
def remAll( e, L ):
    """ removes all
    if len(L) == 0:
        return L
    elif L[0] != e:
        return L[0:1] + remAll(e, L[1:])
    else:
        return remAll(e, L[1:])
```

If there are no elements or characters in L, we're done – return L itself!

from L """

# Design ~ code

5 [7,5,42]

`remAll(e, L)`

*remove all e's from L*

Top-down  
design

Re-Visualize *in syntax!*?

```
def remAll( e, L ):
    """ removes all it L """
    if len(L) == 0:
        return L
    elif L[0] != e:
        return L[0:1] + remAll(e, L[1:])
    else:
        return remAll(e, L[1:])
```

If it is not e, L

USE it (keep it in the return value)

AND remove all the e's from the rest of L!

# Design ~ code

7 [7,5,42]

`remAll(e, L)`

*remove all e's from L*

Top-down  
design

Re-Visualize *in syntax!*?

```
def remAll( e, L ):
    """ removes all e's from L """
    if len(L) == 0:
        return L
    elif L[0] != e:
        return L[0] + remAll(e, L[1:])
    else:
        return remAll(e, L[1:])
```

If it is e,

LOSE it (don't keep it in the return value)

AND still remove all of the e's from the rest of L!

`remAll(e, L[1:])`



Design ~ code

remAll(e, L)

That's it. *Algorithmic expression* ~  
it's what CSers do.  
(think we)

we visualize *in syntax*!?

```
def remAll( e, L ):
    """ removes all e's from L """
    if len(L) == 0:
        return L
    elif L[0] != e:
        return L[0:1] + remAll(e, L[1:])
    else:
        return remAll(e, L[1:])
```

# remAll insight

```
def remAll( e, L ):
    """ removes all e's from L """
    if len(L) == 0:
        return L
    elif L[0] != e:
        return L[0:1] + remAll(e, L[1:])
    else:
        return remAll(e, L[1:])
```

syntax

**remAll(8, [7, 8, 9, 8])** → **[7, 9]**  
                          0  1  2  3

sharpening our model for where + how actions happen...

# other **rem** examples...

`remAll(8, [7, 8, 9, 8])` → `[7, 9]`

**remAll**

`remAll('d', 'coded')` → `'coe'`

**remAll**

`remOne(8, [7, 8, 9, 8])` → `[7, 9, 8]`

**remOne**

`remOne('d', 'coded')` → `'coed'`

**remOne**

`remUpto(8, [7, 8, 9, 8])` → `[9, 8]`

**remUpto**

`remUpto('d', 'coded')` → `'ed'`

**remUpto**

# Subsequences!

*in order*, but not necessarily adjacent...

def subseq( **s**, **sbig** ) → True or False?

**s** is the subsequence  
to find (or not)

**sbig** is the bigger string in  
which we are looking for **s**

subseq( '', 'cataga' ) → True

subseq( 'ctg', 'cataga' ) → True

subseq( 'ctg', 'tacggta' ) →

subseq( 'aliens', 'always frighten dragons' ) →

subseq( 'trogdor', 'that dragon is gone for good' ) →

T or F?

Here there be  
NO dragons!

*Why* Are these True? or False?



# Try it...

# Algorithm design

# Quiz

```
def remAll( e, L ):
    """ removes all e's from L """
    if len(L) == 0:
        return L
    elif L[0] != e:
        return L[0:1]
    else:
        return remAll( e, L[1:] )
```

```
remOne( 8, [7, 8, 9, 8] ) → [7, 9, 8]
```

**1**  
Change `remAll` so that it removes only one `e` from `L`. (We could call it `remOne`.)

**Hint:** remove one thing for `remOne`!

**Hint:** remove one more thing for `remUpto`!

what's needed is mostly crossing stuff out!  
*What stuff?*

**2**  
Make *more* changes to `remAll` so that it removes all of the elements up to and including the first `e` in `L`. (We could call it `remUpto`.)

```
remUpto( 'd', 'coded' ) → 'ed'
```

If `e` is not in `L`, `remUpto` should remove *everything*...

```
def subseq( s, sbig ):
    """ returns True if s is a subseq. of sbig,
        False otherwise. Both are strings.
    """
    if s == '':
        return True
    elif
```

**Challenge...**  
**3** Write the other cases needed for `subseq`...

```
subseq( 'alg', 'magical' )
else
subseq( 'alg', 'twasbrillig' )
True
```

**Hint:** you'll need 3-4 cases total for `subseq`.



Try it...

# Algorithm design

Names: \_\_\_\_\_

```
def remAll( e, L ):
    """ removes all e's from L """
    if len(L) == 0:
        return L
    elif L[0] != e:
        return L[0:1] + remAll(e,L[1:])
    else:
        return remAll(e,L[1:])
```

1

Change `remAll` so that it removes only one `e` from `L`. (We could call it `remOne`.)

```
remOne(8, [7, 8, 9, 8]) → [7, 9, 8]
```

Hint: In both 1 + 2, what's needed is mostly crossing stuff out!

What stuff?

2

Make *more* changes to `remAll` so that it removes all of the elements up to and including the first `e` in `L`. (We could call it `remUpto`.)

```
remUpto('d', 'coded') → 'ed'
```

If `e` is not in `L`, `remUpto` should remove *everything*...

```
def subseq( s, sbig ):
    """ returns True if s is a subseq. of sbig,
        False otherwise. Both are strings.
    """
    if s == '':
        return True
    elif
```

Challenge...

3

Write the other cases needed for `subseq...`

```
subseq('alg', 'magical')
False
```

```
subseq('alg', 'twasbrillig')
True
```



# from remAll to remOne

Hint: remove one thing for remOne!

```
def remAll( e, L ):
    """ returns seq. L with all e's rmovd
    """
    if len(L) == 0:
        return L

    elif L[0] != e:
        return L[0:1] + remAll( e, L[1:] )

    else:
        return remAll( e, L[1:] )
```

Is remAll really "an algorithm"?

Wait! I see One  
more error!



remOne(8, [7, 8, 9, 8]) → [7, 9, 8]

remOne('d', 'coded') → 'coed'

# from remAll to remOne

Hint: remove one thing for remOne!

```
def remAllOne( e, L ):
    """ returns seq. L with all e's rmovd
    """
    if len(L) == 0:
        return L

    elif L[0] != e:
        return L[0:1] + remOne( e, L[1:] )

    else:
        return remAll( e, L[1:] )
```

Wait! I see One  
more error!



remOne(8, [7, 8, 9, 8]) → [7, 9, 8]

remOne('d', 'coded') → 'coed'



# from remOne to remUpto

Hint: remove one more thing for remUpto!

```
Upto
def remOne( e, L ):
    """ returns seq. L with one e removed
    """
    if len(L) == 0:
        return L

    elif L[0] != e:
        return L[0:1] + remUpto( e, L[1:] )

    else:
        return L[1:]
```

I <3 remSleep!



remUpto(8, [7,8,9,8]) → [9,8]

remUpto('d', 'coded') → 'ed'

# from remOne to remUpto

Hint: remove one more thing for remUpto!

```
Upto
def remOne( e, L ):
    """ returns seq. L with one e removed
    """
    if len(L) == 0:
        return L

    elif L[0] != e:
        return L[0:1] + remUpto( e, L[1:] )

    else:
        return L[1:]
```

I <3 remSleep!



remUpto(8, [7,8,9,8]) → [9,8]

remUpto('d', 'coded') → 'ed'

# Subseq ~ coding it out...

```
def subseq( s, sbig ):  
    """ returns True if s is a subseq. of sbig;  
        False otherwise. Both are strings.  
    """  
    if s == '':  
        return True  
    elif s[0]
```

*it*

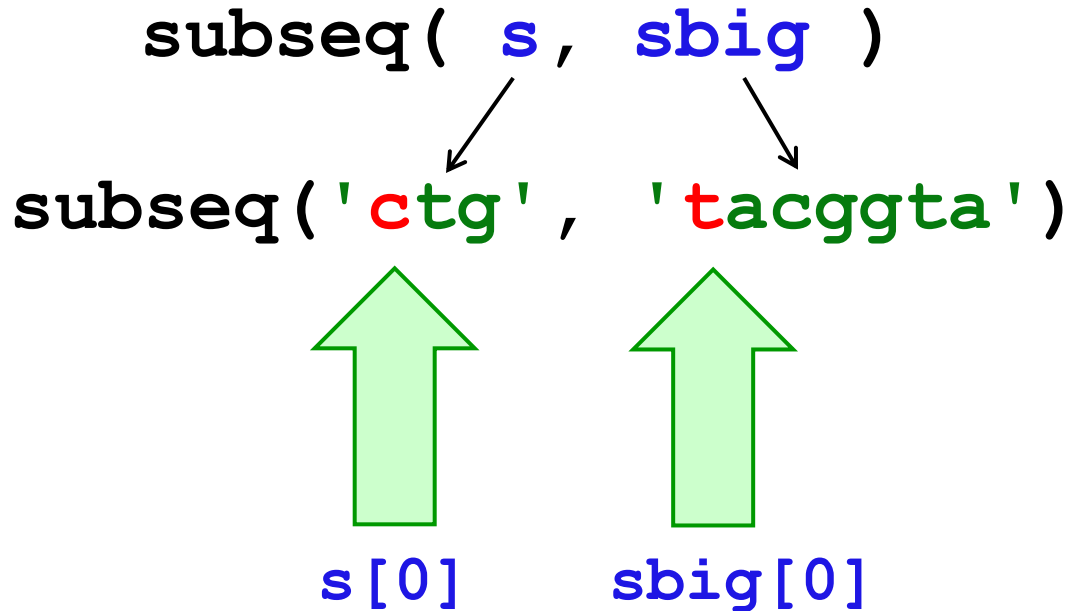
Base case(s)

but first, algorithms!

Recursive step(s)

Where are the *useit* and *loseit* here?

# Subseq ~ *thinking* it out...



What is a small (initial) piece of the problem?  
How would we describe it in terms of the inputs?

**Use it!**

- or -

**Lose it!**

What is left after handling this piece?  
***Are there other functions we will need?***

Top-down  
design

Visualize  
Split into parts

Build each part

Combine  
Test

# Subseq ~ coding it out...

```
def subseq( s, sbig ):  
    """ returns True if s is a subseq. of sbig;  
        False otherwise. Both are strings.  
    """  
    if s == '':  
        return True  
    elif s[0]
```

*it*

Base case(s)

Recursive  
step(s)

Where are the *useit* and *loseit* here?

# Subseq ~ coding it out...

```
def subseq( s, sbig ):  
    """ returns True if s is a subseq. of sbig;  
        False otherwise. Both are strings.  
    """  
    if s == '':  
        return True  
    elif s[0] not in sbig:  
        return False  
    elif s[0] == sbig[0]:  
        return subseq( s[1:], sbig[1:] )  
    else:  
        return subseq( s[0:], sbig[1:] )
```

*it*



Base case(s)

Recursive  
step(s)

Where are the *useit* and *loseit* here?

# Subseq ~ coding it out...

```
def subseq( s, sbig ):  
    """ returns True if s is a subseq. of sbig;  
        False otherwise. Both are strings.  
    """  
    if s == '':  
        return True  
    elif s[0] not in sbig:  
        return False  
    else:  
        return subseq( s[1:], remUpto( s[0], sbig) )
```

*it*

Base case(s)

rest of s

rest of sbig after s[0]

Recursive  
step(s)

Where are the *useit* and *loseit* here?

# Subseq ~ coding it out...

```
def subseq( s, sbig ):  
    """ returns True if s is a subseq. of sbig;  
        False otherwise. Both are strings.  
    """  
    if s == '':  
        return True  
    elif s[0] not in sbig:  
        return False  
    else:  
        return subseq( s[1:], reupto( s[0], sbig ) )
```

*it*

Base case(s)

"Use it or lose it"

Recursive  
step(s)

Where are the *useit* and *loseit* here?

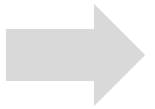


**Design** ~ *(code)*

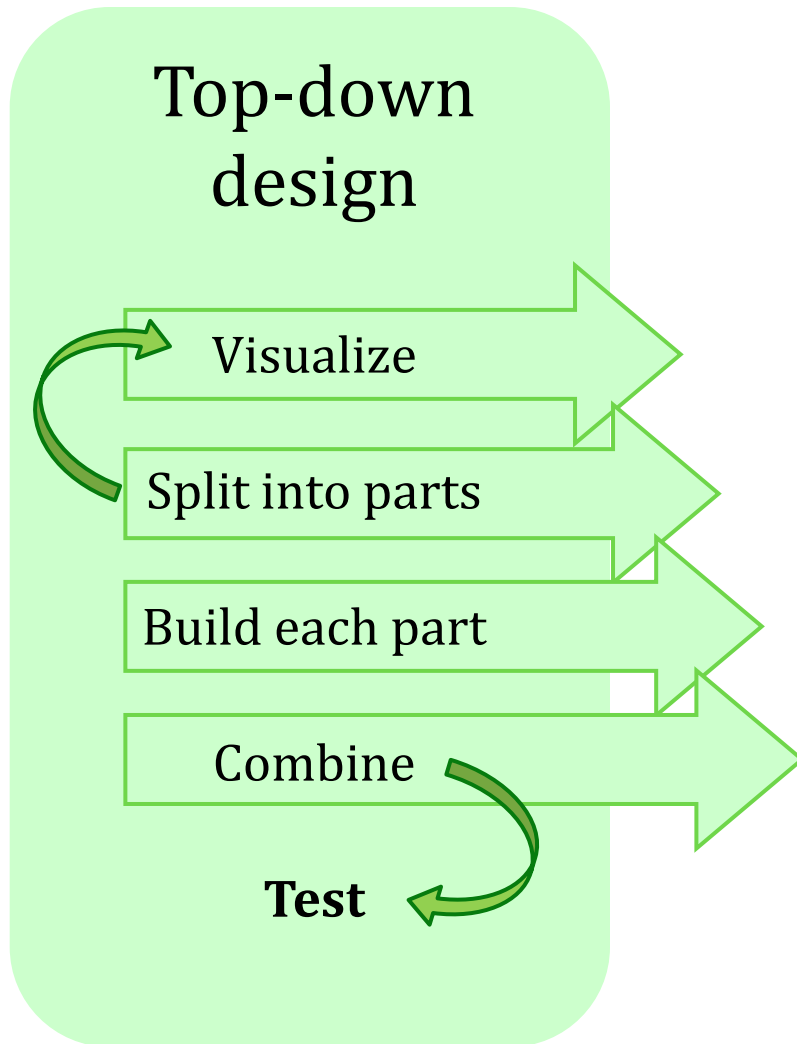
That's it. *Algorithmic expression* ~  
it's what CSers *think they do*.

*... at this  
moment in a  
prior CS5 ...*

**it** can take some  
"getting used to" ... ?

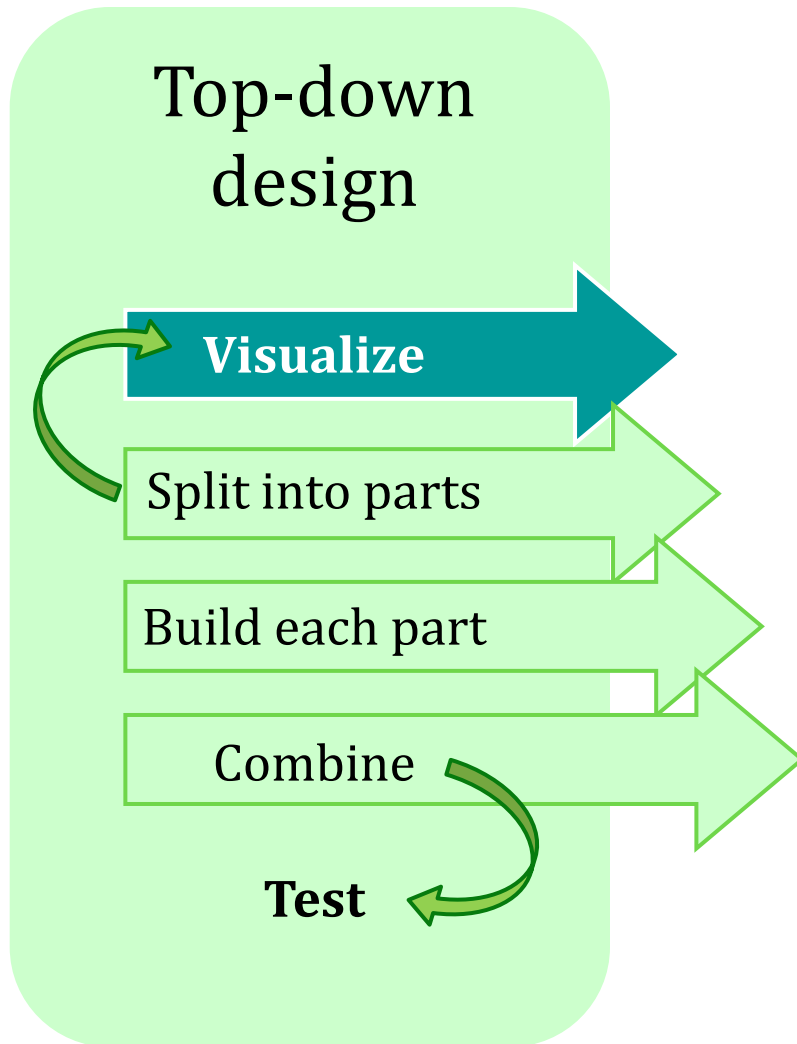


# What's the *problem*?!



*Which one of these steps is the most important?*

# *What's the problem?!*



*understanding  
what the problem  
demands!!*

*I want some examples!*



## hw3pr2: *use-it-or-lose-it* algorithm design

Longest **C**ommon **S**ubsequence

LCS( S, T )

Jotto **S**core counting

jscore( s1, s2 )

**b**inary list and  
**g**eneral list **s**orting

blsort( L ), gensort( L )

**e**xact\_**c**hange making

exact\_change( t, L )

# hw3pr2: *use it or lose it*

Longest Common Subsequence

LCS( S, T )

'BONOBO'

'CHIMPANZEE'

'CGCTGAGCTAGGCA...'

'ATCCTAGGTAAGT...'

+10<sup>9</sup> more

Eye oneder if this haz  
other aplications?



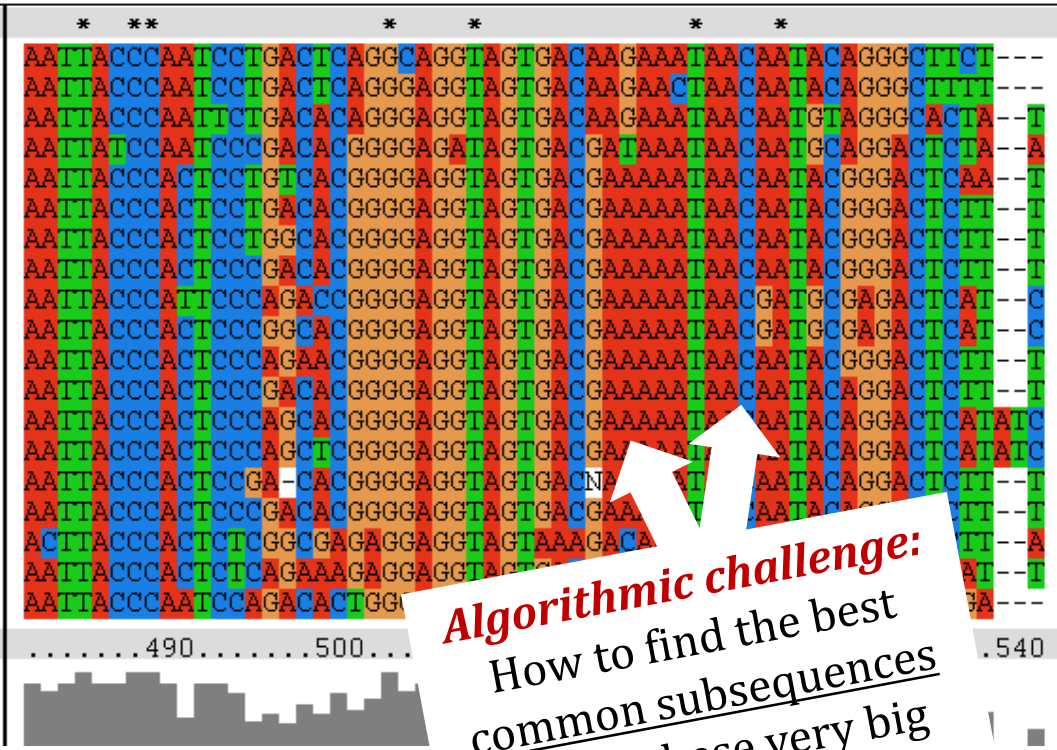
# Why LCS?

Screenshot from the ClustalX multiple subsequence alignment tool...

Multiple Alignment Mode Font Size: 10



- 1 Metridium
- 2 A.sulcata
- 3 Hematodinium
- 4 S.raphanus
- 5 N.virens
- 6 L.latreilli
- 7 Modiolus
- 8 S.solidissima
- 9 Pagurus
- 10 Emerita
- 11 Coelotes
- 12 F.heteroclitus
- 13 Chrysops
- 14 D.simulans
- 15 S.purpuratus
- 16 A.forbesi
- 17 G.rhodei
- 18 A.crucifera
- 19 M.portucalensis
- ruler



**Algorithmic challenge:**  
 How to find the best  
common subsequences  
 among these very big  
 genome strings !?!

# also in hw3pr2: *Jotto* !

a word-guessing game...

jscore( S, T )

YOUR SECRET JOTTO WORD			OPPONENT'S SECRET JOTTO LETTERS		
MAPLE			WNGOR		
JOTTO™					
SCORE	OPPONENT'S TEST WORD	NO. OF JOTS	YOUR TEST WORD	NO. OF JOTS	
100	FLASK	2	WHALE	1	
95	LULLS	1	SHAKE	0	
90	PLUMP	3	FLING	2	
85	SLUMP	3	FLUNG	2	
80	LYMPH	3	SLANG	2	
75	NYMPH	2	GROAN	4	

# jscore

*"Jotto scoring"*

These are  
two cute



'robot'



'otter'

`jscore( 'robot', 'otter' ) →`

`jscore( S, T )`

*Let's try it!*



also in hw3pr2: **sort + exact\_change**

**sort( [42,5,7] )** → **[5,7,42]**

**sort( [42,7] )** → **[7,42]**

**sort( [42] )** → **[42]**

returns an ascending list

---

**exact\_change( 42, [25,30,2,5] )** → **False**

**exact\_change( 42, [25,30,2,15] )** → **True**

returns **True** or **False**

should return the jotto score for any strings **S** and **T**

## jscore ( S , T )

jscore('robot', 'otter') → 3  
 jscore('geese', 'seems') → 3  
 jscore('fluff', 'lulls') → 2  
 jscore('pears', 'diner') →   
 jscore('xylyl', 'slyly') →

Extra! Which of these 10 is the *cruellest* hidden jotto word?

should return a new list that is the sorted version of the input **L**

## sort ( L )

sort( [42,5,7] ) → [5,7,42]  
 sort( [42,7] ) → [7,42]  
 sort( [42] ) → [42]  
 sort( [ ] ) →   
 blsort( [1,0,1] ) →

binary-list sort:  
same as sort, but all of the #s are 0 or 1

should return the Longest Common Subsequence of strings **S** and **T**

## LCS ( S , T )

LCS( 'ctga', 'tagca' ) → 'tga'  
 LCS( 'tga', 'taacg' ) → 'ta' (or 'tg')  
 LCS( 'tga', 'a' ) →   
 LCS( 'gattaca', 'ctctgcgat' ) →

Use it!  
 Lose it!  
**remOne**  
 how is remOne used?

don't write any code for these...

min  
**remOne**  
 how are min and remOne used?

do answer examples + brainstorm

Use it!  
 Lose it!  
 Lose it!  
**only recursion here...**  
 this is eerily like svTree

# Brainstorm algorithms for these problems. What helper functions?? might help for each...

returns True if **any** subset of elements in L add up to t; returns False otherwise

## exact\_change ( t , L )

exact\_change( 42, [25,30,2,5] ) → False  
 exact\_change( 42, [22,16,3,2,17] ) →   
 exact\_change( 42, [18,21,22] ) →   
 exact\_change( 42, [40,17,1,7] ) →   
 exact\_change( 20, [16,3,2,17] ) →

Use it!  
 Lose it!  
**... and here**

should return the jotto score for any strings  $s_1$  and  $s_2$

## jscore(s1, s2)

jscore('robot', 'otter') → 3

jscore('geese', 'seems') → 3

jscore('fluff', 'lulls') → 2

jscore('pears', 'diner') → 2

jscore('xylyl', 'slylyl') → 4

Extra! Which of these 10 is the *cruellest* hidden jotto word?

should return a new list that is the sorted version of the input  $L$

## sort(L)

sort([42,5,7]) → [5,7,42]

sort([42,7]) → [7,42]

sort([42]) → [42]

sort([]) → []

bsort([1,0,1]) → [0,1,1]

binary-list sort:  
same as sort, but all of the #s are 0 or 1

should return the Longest Common Subsequence of strings  $S$  and  $T$

## LCS(S, T)

LCS('ctga', 'tagca') → 'tga'

LCS('tga', 'taacg') → 'ta' (or 'tg')

LCS('tga', 'a') → 'a'

LCS('gattaca', 'ctctgcgat') → 'ttca'

4 chars

Use it!

Lose it!

remOne

how is remOne used?

don't write any code for these...

min

remOne

how are min and remOne used?

do answer examples + brainstorm

Use it!

Lose it!

Lose it!

only recursion here...

this is eerily like svTree

Brainstorm algorithms for these problems. What **helper functions???** might help for each...

returns True if **any** subset of elements in  $L$  add up to  $t$ ; returns False otherwise

## exact\_change(t, L)

exact\_change(42, [25,30,2,5]) → False

exact\_change(42, [22,16,3,2,17]) → True

exact\_change(42, [18,21,22]) → False

exact\_change(42, [40,17,1,7]) → False

exact\_change(20, [16,3,2,17]) → True

Use it!

Lose it!

... and here

decipher( 'Weet bksa ed xecumeha 3!' )

kxn rkfo k qbokd goouoxn ...

decipher( 'Weet bksa ed xecumeha 3!' )



Good luck on homework 3!

kxn rkfo k qbokd goouoxn ...



and have a great weekend ...

